Mathematics Textbooks with Open Licenses

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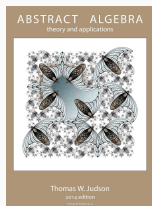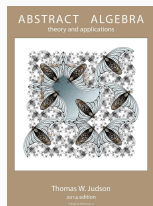 - Possibly: the right to distribute modifications
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An Open Textbook, Online

Abstract Algebra: Theory and Applications, by Tom Judson

- #2 in Google "`abstract algebra`"
- Openly licensed
- Hardcopy: R 300 (USD 25)
- PDF download: Free! (Legally!)
- Online: Includes Sage Cell examples

Web Versions of Open Textbooks

- Portable: 64 GB is
  - 64 Encyclopedia Britannica (text)
  - 1 English Wikipedia (text)
  - 10,000 400-page math textbooks (w/ images)

- Ubiquitous: laptop, tablet, or phone

- Up-to-Date: correct, and refresh, at will

- Accurate: crowd-sourced proof-reading

- Open: never out-of-print

- Intellectually Honest:
  no pressure to satisfy market segments

- **FREE!!!!!**


THIS WAS GOOGLE
WHEN I WAS A KID

Proprietary Electronic Textbooks

- Expire after course
- Limited printing
- Inconvenient interfaces
- Difficult to resell
- Page-oriented (ala PDF)

Interactive Web Versions

- Extensive cross-referencing, index
- Information hiding ("knowls")
- Acessibility features
- MathJax for math, Google for fonts
- Integrated Google Search
- Embedded YouTube Videos
- Interactive demonstrations: Sage, Python, GeoGebra, CalcPlot3D, Desmos, JSXGraph
- Live, instant-response, homework: WeBWorK, MyOpenMath, two others in development
- Offline? PDF, EPUB, or talk to me
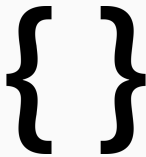
ABSTRACT ALGEBRA DEMONSTRATION
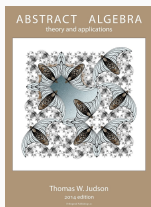
The Movement

KEY INSIGHT #3: MATHEMATICS AND STATISTICS IS THE ACADEMIC SUBJECT WITH THE MOST OER TRACTION

Institutions were asked to note which academic subjects had the greatest OER traction. Amongst the 65 institutions that answered this question, mathematics and statistics ranked the highest with nearly half (30) indicating it had traction, followed by social and behavioural sciences (22), biological and related sciences (21), and chemistry (20). Figure 6 depicts the top 10 academic subjects with the most OER traction.

Figure 6. Top 10 academic subjects with the most OER traction.
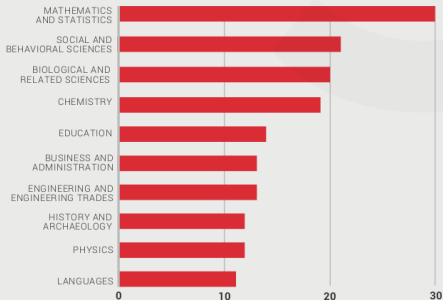
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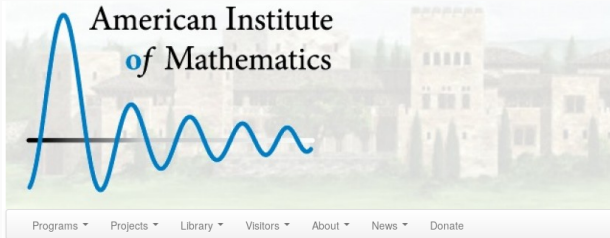
Approved Textbooks • Evaluation Criteria • Guide for Authors • Editorial Board

Approved Textbooks

The list below groups open textbooks by course title. All the books have been judged to meet the evaluation criteria set by the AIM editorial board.

⌄ **Liberal Arts Math**

⌄ **College Algebra and Precalculus**

⌄ **Calculus**

⌄ **Differential Equations**

⌄ **Linear Algebra**

⌄ **Introduction to Proofs**

⌄ **Discrete Math**

⌄ **Combinatorics**

⌄ **Mathematical Computing**

⌄ **Numerical Analysis**

⌄ **Abstract Algebra**

⌄ **Number Theory**

⌄ **Real Analysis**

⌄ **Complex Analysis**

⌄ **Geometry and Topology**

⌄ **Probability**

⌄ **Statistics**

⌄ **Logic**

AIM Open Textbook Initiative

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⌄ **Linear Algebra**

⌄ **Introduction to Proofs**

⌄ **Discrete Math**

⌃ **Combinatorics**

Applied Combinatorics
Mitchel T. Keller and William T. Trotter

Combinatorics Through Guided Discovery
Kenneth Bogart

Foundations of Combinatorics with Applications
Edward A. Bender and S. Gill Williamson

⌄ **Mathematical Computing**

⌄ **Numerical Analysis**

⌄ **Abstract Algebra**

⌄ **Number Theory**

⌄ **Real Analysis**

⌄ **Complex Analysis**

⌄ **Geometry and Topology**

⌄ **Probability**

⌄ **Statistics**

⌄ **Logic**

Bogart's Combinatorics Through Guided Discovery

Combinatorics Through Guided Discovery

Kenneth P. Bogart

Digital versions	PDF and HTML
PreTeXt source	Yes
Exercises	Yes
Solutions	Solution manual available to instructors
License	GNU Free Documentation License

- Text for a first course in combinatorics
- Copyright 2004 by author
- 200 pages, 6 chapters, 3 supplemental sections
- Over 400 exercises, many with hints
- Paperback version available for about $9
- For more information and to access PDF or online version

As the title suggests this book is designed for a "discovery method" course. The heart of the book is the hundreds of exercises that guide the student through the key ideas of enumerative combinatorics and a brief introduction to graph theory. The exercises are marked with special symbols to indicate their role in the course, for example, whether they are essential or motivational. The chapter titles are

1. What is Combinatorics?
2. Applications of Induction and Recursion in Combinatorics and Graphy Theory
3. Distribution Problems
4. Generating Functions
5. The Principle of Inclusion and Exclusion
6. Groups Acting on Sets

The three supplmental sections deal with relations, mathematical induction, and exponential generating functions.

This book is the result of an NSF project led by Ken Bogart and is currently maintained by the Mathematics Department of Dartmouth College.

PreTeXt

PreTeXt Authoring Language

- Philosophy: **rigorously** separate
  - structure and content
  - presentation

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  - math content: still LaTeX (AMS Math)
- Payoff:
  - multiple outputs from a single source
  - powerful and flexible processing with eXtensible Stylesheet Language (XSL)
  - author with your favorite text editor
  - cross-platform open-source toolchain

New Author-Friendly XML Vocabulary

- Sensible element names
  - book, chapter, section, subsection
  - theorem: title, statement, proof
- Sensible abbreviations
  - p, ul, ol, dl, li, q, em
  - m, me, md/mrow
- Consistent element use
  - title
  - introduction
  - xref, xml:id
- Only three dangerous characters: &, $<$, $>$
- Simple rules for special (escaped) characters
- Schema for element relationships, validation

PreTeXt Example

```
<theorem xml:id="power-rule">
    <title>Power Rule</title>
    <idx>power rule</idx>

    <statement>
        <p>The derivative of <m>f(x)=x^n</m>
        is <m>f'(x)=nx^{n-1}</m>.</p>
    </statement>

    <proof>
        <p>Apply induction to the product
            <me>f(x)=x^n=x\cdot x^{n-1}</me>
        using <xref ref="product-rule"/>.</p>
    </proof>
</theorem>
```

Theorem 4.4 (Power Rule). *The derivative of $f(x) = x^n$ is $f'(x) = nx^{n-1}$.*

Proof. Apply induction to the product

$$f(x) = x^n = x \cdot x^{n-1}$$

using Theorem 4.1. □

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Proof. Apply induction to the product

$$f(x) = x^n = x \cdot x^{n-1}$$

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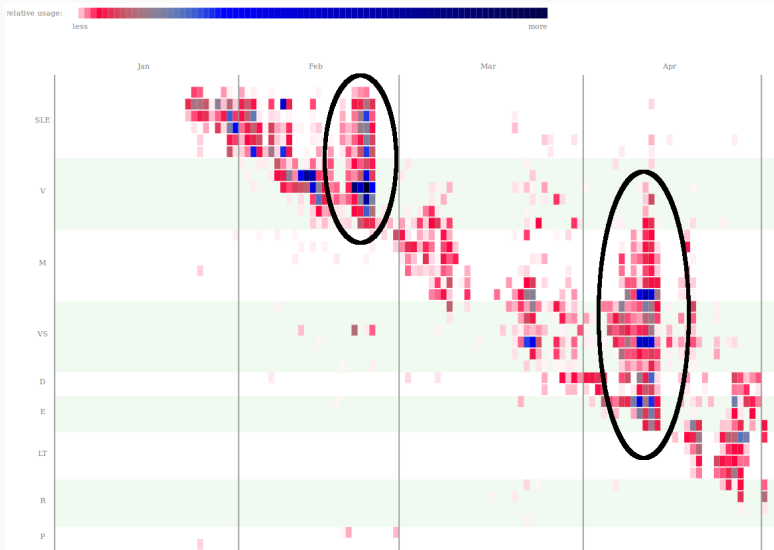
Corollary 4.5. *Suppose $f(x)$ is a continuous function. Then*

What's New?

Textbook Use: All Students for Entire Semester

Rows are sections, columns are days
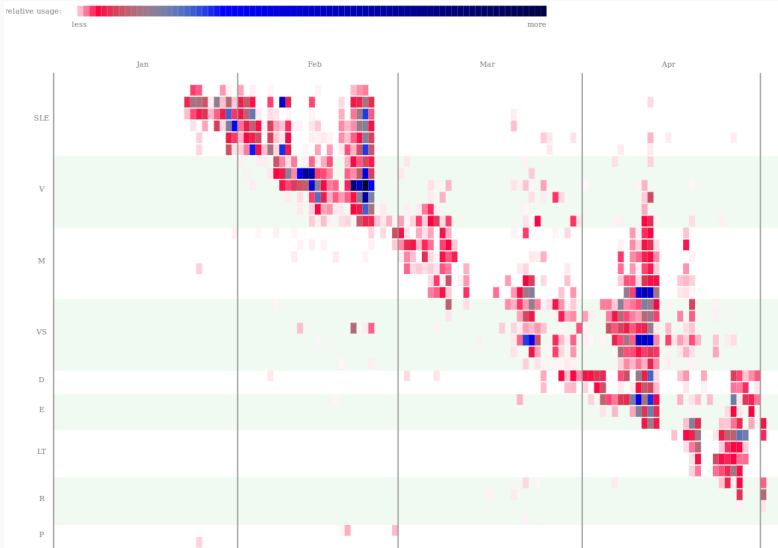
Rows are sections, columns are days

Rows are sections, columns are days

MyOpenMath Embedded Problems

Julia in a Jupyter Notebook on CoCalc

Thank-you for your attention

PreTeXt: `mathbook.pugetsound.edu`

`buzzard.pugetsound.edu/talks.html`