Research Project   As a portion of your work in this advanced course you will carefully research a topic or application in abstract algebra (including group theory), to present in writing and to the class.

Subject   Any topic that extends our understanding of abstract algebra, or makes heavy use of abstract algebra in an application, is a legitimate subject. However, you must have your topic approved to avoid duplication with course material or other students' presentations. Send me an email once you have settled on a topic to "claim" it. If you use a topic that has been done before, your work must be substantially different.

Proposal   A one-page proposal is due before class on March 9. This should provide evidence that you have a viable subject and are not duplicating course material or another student's subject. A preliminary bibliography of primary sources will provide the best evidence that you have given your subject adequate consideration. These will be returned quickly, and once approved you may schedule your presentation for a time slot during the final four days of the semester.

Written Report   Your full written report will be due April 16 before class. As a rough guideline, I will be expecting 8 to 10 pages (assuming normal margins and spacing). I will circulate this report to your classsmates prior to your oral presentation. These will also be posted on the course web page, so you will need to determine what license you will use along with your copyright.

Oral Report   You will give a 25-minute presentation to the class, accompanied with slides created with TEX and Beamer.

Tools   Your proposal and written report will be in PDF format, created with TEX. Your presentation will be accompanied with slides created in TEX with the Beamer package. See me if you need help learning these tools.

Grading   This project represents 15% of your course grade, partitioned as follows: Proposal approved on-time – 2%, Written Report – 8%, Oral Report – 5%. Attendance at your peers' presentations is an integral part of this course. Therefore you will be allowed only one absence for any reason, and any additional absences will result in a 1% grade penalty on your own project score. Portions submitted electronically can be emailed to the usual address for reading questions and Sage exercises.

Date	Component	Format
Mar 9	Proposal	1-page TEX PDF via email
Apr 16	Written Report	TEX PDF via email
Apr 24–May 1	Oral Report	Beamer PDF, email in advance

Topic Suggestions

In no particular order. Some topics are very specific, and some of these are very technical. Others are very general and might be approached as providing an introduction, or survey, of the topic.

- Advanced Encryption Standard (AES). Encryption, uses irreducible polynomials, finite fields.

- Orders in Rings. `http://www-math.mit.edu/~kedlaya/Math254B/Orders.pdf`

- Quaternion Algebras. Survey properties, etc.

- Noetherian Rings, Artinian Rings. One, or both.

- Cyclotomic Fields, Cyclotomic Extensions. (Without duplicating course material.)

- Formal Power Series, Laurent Series. One, or both. Laurent Series allow negative-exponent terms.

- Motzkin paper on $\mathbf{Q}[\sqrt{d}]$, `http://projecteuclid.org/handle/euclid.bams/1183514381`

- Composition Algebras. Quaternions, Octonions.

- Resultant of two polynomials, Sylvester Matrix. Related to roots of polynomials.

- Noncommutative Rings. Survey what happens if we drop commutativity, e.g. one-sided ideals.

- Modules. "Vector spaces over rings." (Without duplicating course material from vector space chapter.)

- p-adic Numbers. From an algebraic viewpoint (not analysis). Application to computer arithmetic?

- Algebras. General survey, examples.

- Algebraic Coding Theory. See Judson, Chapters 7 and 20 for a start.

- Burnside's Counting Theorem, Polya's Enumeration Theorem. See Judson, Chapter 12, for a start.

- Finite Groups of Order 16. (I have no idea how ambitious this is.)

- Dicyclic Groups.

- Gröbner Bases. (For ideals, see Fraleigh, 7e, Section 28)

- Todd-Coxeter Coset enumeration. (Computer algebra.)